## APPENDIX B: TECHNICAL NOTES

## VITAL STATISTICS FORMULAS

## Age-Adjusted Rates

Age-adjusted rates are calculated so comparisons can be made between populations that have different age distributions. For example, " X " population which has a relatively high proportion of young people, generally will experience a lower crude death rate than " $Y$ " population which is made up of a relatively high percentage of elderly. Age-adjusted rates are more appropriate than crude rates when comparing health indicators for populations that have different age distributions. The age-adjusted rates in this report were calculated using the standard million population based on the decennial U.S. Census of 1940. (See Standard Million Population in Appendix A.)

$$
\begin{aligned}
& \text { age-adjusted death rate }=\sum m_{a}\left(P_{a} / p\right) \\
& \text { where: } \quad \begin{array}{l}
\Sigma \text { is sum } \\
m_{a} \text { is the age-specific death rate } \\
\\
P_{a} \text { is the standard population for the age group } \\
\\
p \text { is the total standard population }
\end{array}
\end{aligned}
$$

## Confidence Intervals

In this report, confidence intervals are used to provide a range within which the true rate will fall with a probability of $95 \%$. The size of the range is determined by the number of occurrences, the base population, and the standard error.

Using teen birth rate by census area as an example, refer to Chart 1.2B:
3 -year births to teens ages $15-19$ in 1994-1996 $=3,437$ (b)
3-year annual female teen population in 1994-1996 $=59,289(p)$
Annual teen birth rate per 1,000 female teens $=(3,437 / 59,289) * 1,000=58.0(R)$
Standard error $=\quad k / \sqrt{b}$
$\mathrm{ci}=\mathrm{R} \pm 1.96(\mathrm{R} / \sqrt{\mathrm{b}})$
$c i=58.0 \pm 1.96(58.0 / \sqrt{3,437}) \quad$ or $c i=56.0-59.9$

We can say, for example, that there is a $95 \%$ probability that the interval from 56.0 to 59.9 contains the true teen birth rate for the State of Alaska for the period 1994-1996.

## Expectation of Life

Expectation of life is the number of years infants born in a specific year can expect to live if they experience the same age-specific death rates experienced during their birth year. Table B. 1 illustrates the calculation of life expectancy for all Alaskans based on data from a five year period.

TABLE B. 1 EXPECTATION OF LIFE FOR ALL ALASKANS, 1992-1996

| $\begin{array}{\|c\|} \text { AGE } \\ \text { AT } \\ \text { DEATH } \\ \hline \end{array}$ | COLUMN IDENTIFICATION AND DESCRIPTION |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | B | C | D | E | F | G | H | I | J |
|  | DTHS | POP | RATIO | $\begin{aligned} & \text { PROPORTION } \\ & \text { DYING IN } \\ & \text { AGE GROUP } \end{aligned}$ | $\begin{aligned} & \text { PROPORTION } \\ & \text { LIVING IN } \\ & \text { AGE GROUP } \end{aligned}$ | NO. LIVING AT BEGINNING OF AGE GROUP | NO. <br> DYING <br> IN AGE <br> GROUP | NUMBER LIVING IN THE AGE GROUP | $\begin{aligned} & \text { CUM } \\ & \text { POP } \\ & \hline \end{aligned}$ | YEARS LEFT AT BEGINNING OF AGE GROUP |
| <1 | 426 | 53,931 | 0.00790 | 0.00787 | 0.99213 | 100,000 | 787 | 99,331 | 7,423,112 | 74.2 |
| 01-04 | 123 | 232,759 | 0.00053 | 0.00211 | 0.99789 | 99,213 | 209 | 396,329 | 7,323,781 | 73.8 |
| 05-09 | 61 | 274,556 | 0.00022 | 0.00111 | 0.99889 | 99,004 | 110 | 494,744 | 6,927,451 | 70.0 |
| 10-14 | 91 | 261,621 | 0.00035 | 0.00174 | 0.99826 | 98,894 | 172 | 494,040 | 6,432,707 | 65.0 |
| 15-19 | 251 | 205,677 | 0.00122 | 0.00608 | 0.99392 | 98,722 | 601 | 492,109 | 5,938,668 | 60.2 |
| 20-24 | 325 | 212,477 | 0.00153 | 0.00762 | 0.99238 | 98,121 | 748 | 488,738 | 5,446,559 | 55.5 |
| 25-29 | 367 | 249,143 | 0.00147 | 0.00734 | 0.99266 | 97,374 | 715 | 485,083 | 4,957,821 | 50.9 |
| 30-34 | 499 | 287,604 | 0.00174 | 0.00864 | 0.99136 | 96,659 | 835 | 481,209 | 4,472,737 | 46.3 |
| 35-39 | 550 | 298,679 | 0.00184 | 0.00917 | 0.99083 | 95,824 | 878 | 476,927 | 3,991,528 | 41.7 |
| 40-44 | 625 | 270,623 | 0.00231 | 0.01148 | 0.98852 | 94,946 | 1,090 | 472,006 | 3,514,601 | 37.0 |
| 45-49 | 642 | 206,694 | 0.00311 | 0.01541 | 0.98459 | 93,856 | 1,446 | 465,665 | 3,042,596 | 32.4 |
| 50-54 | 673 | 142,344 | 0.00473 | 0.02336 | 0.97664 | 92,410 | 2,159 | 456,651 | 2,576,931 | 27.9 |
| 55-59 | 798 | 95,756 | 0.00833 | 0.04082 | 0.95918 | 90,251 | 3,684 | 442,044 | 2,120,280 | 23.5 |
| 60-64 | 988 | 71,126 | 0.01389 | 0.06712 | 0.93288 | 86,567 | 5,811 | 418,308 | 1,678,236 | 19.4 |
| 65-69 | 1204 | 54,348 | 0.02215 | 0.10495 | 0.89505 | 80,756 | 8,476 | 382,592 | 1,259,928 | 15.6 |
| 70-74 | 1279 | 39,324 | 0.03252 | 0.15039 | 0.84961 | 72,280 | 10,871 | 334,226 | 877,337 | 12.1 |
| 75-79 | 1163 | 22,433 | 0.05184 | 0.22947 | 0.77053 | 61,410 | 14,092 | 271,819 | 543,111 | 8.8 |
| 80-84 | 1047 | 12,199 | 0.08583 | 0.35332 | 0.64668 | 47,318 | 16,718 | 194,793 | 271,292 | 5.7 |
| 85+ | 1251 | 8,704 | 0.14373 | 0.52867 | 0.47133 | 30,599 | 30,599 | 76,499 | 76,499 | 2.5 |

Column A: total deaths during five years.
Column B: sum of population for each of the five years.
Column C: ratio. A/B
Column D: proportion dying in the age group. For less than 1 year: $\left(2^{*} C\right) /(2+C)$; for $1-4$ years: $\left(2^{*} 4^{*} C\right) /\left(2+4^{*}\left(1.25^{*} C\right)\right)$; all others: $\left(2^{*} 5^{*} C\right) /\left(2+5^{*} C\right)$
Column E: proportion living in age group. 1-D
Column F: number living at beginning of age. For less than 1 year: 100,000; all others: $\mathrm{E}^{\star} \mathrm{F}$ (both from next younger age group)
Column $G$ : number dying in the age group. $F$ (this age group) $-F$ (next older age group)
Column H: number living in the age group. For less than 1 year: $\mathrm{F}-\left(.85^{*} \mathrm{G}\right)$; for $1-4$ years: $4^{*} \mathrm{~F}-\left(2.5^{*} \mathrm{G}\right)$; all others: $\left(5^{*} \mathrm{~F}\right)-\left(2.5^{*} \mathrm{G}\right)$
Column I: cumulative population. Sum of H for this and all older age groups
Column J: years left at beginning of age. I/F

## Moving Averages

Calculations of 3-year, 5-year, and 10-year moving averages are performed when single-year rates are not reliable. Often when small numbers are used for calculations, use of moving averages helps to smooth out rates which vary randomly from one period to another.

For example, single-year infant mortality rates are seldom good indicators of the state of health within populations because rates can fluctuate dramatically from year to year. In Alaska, 132 infants died during 1988 and 108 infants died during 1989. The single-year infant mortality rates during 1988 and 1989 were 11.7 and 9.3, respectively. The 3 -year moving average IMR (using 1986, 1987, and 1988 data) was 11.0 and (using 1987, 1988, and 1989) 10.4 infant deaths per 1,000 live births.

## Years of Life Lost

Years of Life Lost (YLL), or Years of Productive Life Lost, is the difference between the standardized age of 65 and the age of a decedent who dies before age 65 . For purposes of calculation, deaths are assumed to occur at the midpoint of a five-year age interval; i.e. a 41-year-old decedent is assumed to be 42.5 years or halfway between 40 and 45. A person dying at age 41 would be said to have 22.5 years of life lost (65-42.5). Years of Life Lost
emphasizes mortality in younger populations and is used in this report to measure the impact of specific causes of death. For a specific decedent group, Years of Life Lost is calculated as follows:

$$
\begin{aligned}
& \text { YLL }=\sum 65-m p \\
& \text { where } \\
& : \\
& \quad \begin{array}{l}
\text { YLL is Years of Life Lost } \\
\\
\\
\\
\\
\\
m p \text { is sum of all decedents' years of productive life lost years of productive life }
\end{array} \\
&
\end{aligned}
$$

